

# Mobile Communications

TCS 455

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**Lecture 22**

**Office Hours:**

**BKD 3601-7**

**Tuesday 14:00-16:00**

**Thursday 9:30-11:30**

# Announcements

- Read
  - Chapter 9: 9.1 – 9.5
- HW5 is posted.
  - Due: Feb 5 (Friday after university game)

# Chapter 5

## OFDM

**Office Hours:**  
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# OFDM

- Some of you already have seen this presentation (from the 1<sup>st</sup> OFDM(A) tutorial.)

# Chapter 5

## OFDM

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# Orthogonality in Communication

CDMA

$$s(t) = \sum_{k=0}^{\ell-1} S_k c_k(t) \xrightarrow{\mathcal{F}} S(f) = \sum_{k=0}^{\ell-1} S_k C_k(f) \quad \text{where } c_{k_1} \perp c_{k_2}$$

TDMA

$$s(t) = \sum_{k=0}^{\ell-1} S_k c(t - kT_s) \xrightarrow{\mathcal{F}} S(f) = C(f) \sum_{k=0}^{\ell-1} S_k e^{-j2\pi f k T_s}$$

where  $c(t)$  is time-limited to  $[0, T]$ .

This is a special case of CDMA with  $c_k(t) = c(t - kT_s)$

The  $c_k$  are non-overlapping in time domain.

FDMA

$$S(f) = \sum_{k=0}^{\ell-1} S_k C(f - k\Delta f)$$

where  $C(f)$  is frequency-limited to  $[0, \Delta f]$ .

This is a special case of CDMA with  $C_k(f) = C(f - k\Delta f)$

The  $C_k$  are non-overlapping in freq. domain.

# OFDM

- Let  $S_1, S_2, \dots, S_N$  be the information symbol.
- The discrete baseband OFDM modulated symbol can be expressed as

$$\begin{aligned} s(t) &= \frac{1}{\sqrt{N}} \sum_{k=0}^{N-1} S_k \exp\left(j \frac{2\pi kt}{T_s}\right), \quad 0 \leq t \leq T_s \\ &= \sum_{k=0}^{N-1} S_k \underbrace{\frac{1}{\sqrt{N}} 1_{[0, T_s]}(t)}_{c_k(t)} \exp\left(j \frac{2\pi kt}{T_s}\right) \end{aligned}$$

Note that:

$$\operatorname{Re}\{s(t)\} = \frac{1}{\sqrt{N}} \sum_{k=0}^{N-1} \left( \operatorname{Re}\{S_k\} \cos\left(\frac{2\pi kt}{T_s}\right) - \operatorname{Im}\{S_k\} \sin\left(\frac{2\pi kt}{T_s}\right) \right)$$

# Chapter 5

## OFDM

Wireless Channel

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# Single Carrier Transmission

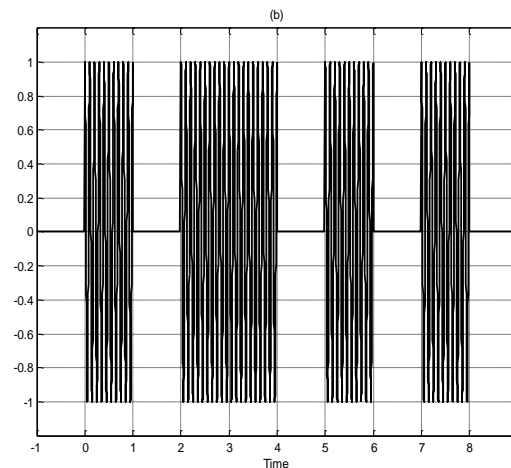
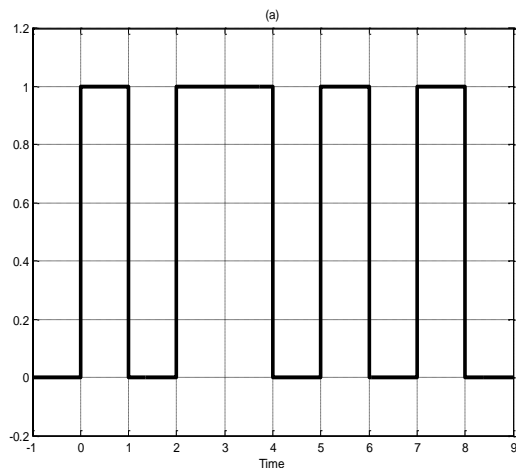
- Baseband:

$$s(t) = \sum_{k=0}^{N-1} s_k p(t - kT_s)$$

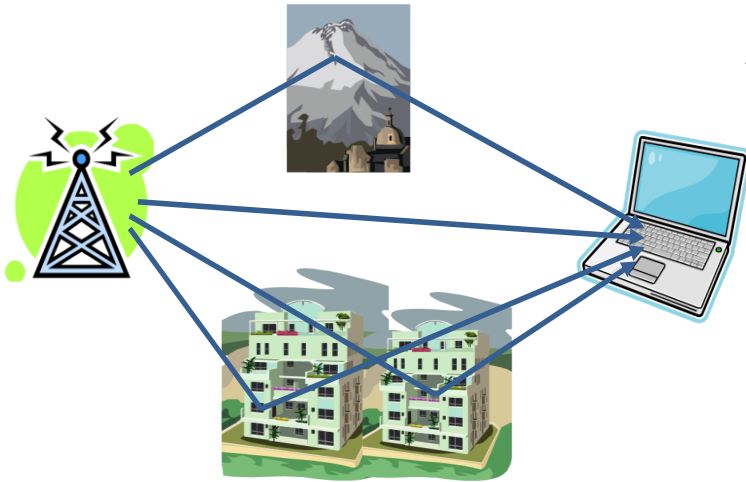
$$p(t) = 1_{[0, T_s)}(t) = \begin{cases} 1, & t \in [0, T_s) \\ 0, & \text{otherwise.} \end{cases}$$

- Passband:

$$x(t) = \text{Re}\{s(t)e^{j2\pi f_c t}\}$$



# Wireless Comm. and Multipath Fading

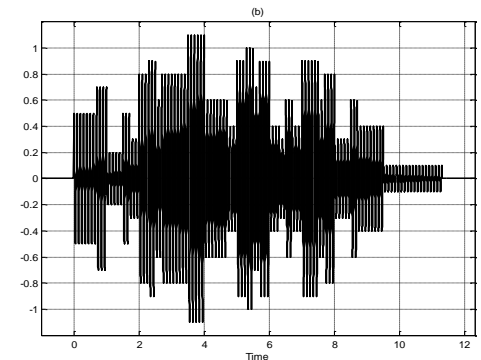
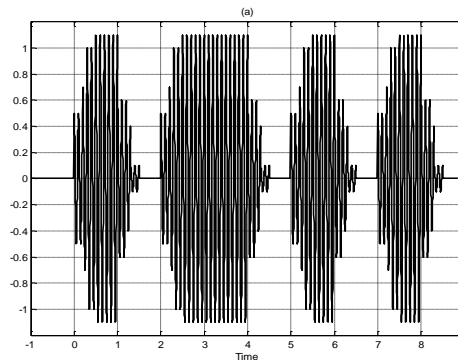
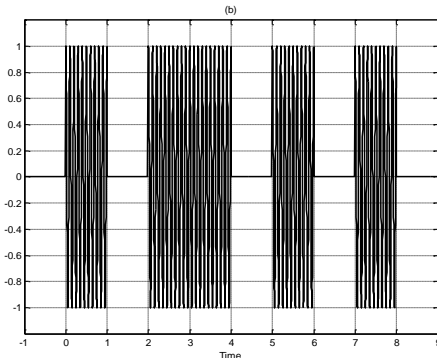


$$r(t) = x(t) * h(t) + n(t) = \sum_{i=0}^v \beta_i x(t - \tau_i) + n(t)$$

$$h(t) = \sum_{i=0}^v \beta_i \delta(t - \tau_i)$$

$$h_1(t) = 0.5\delta(t) + 0.2\delta(t - 0.2T_s) + 0.3\delta(t - 0.3T_s) + 0.1\delta(t - 0.5T_s)$$

$$h_2(t) = 0.5\delta(t) + 0.2\delta(t - 0.7T_s) + 0.3\delta(t - 1.5T_s) + 0.1\delta(t - 2.3T_s)$$



# Frequency Domain

